

SI Physics - Full Discipline Demo

Refractive Index of a Glass Slab

Final Report - Answer Guide

Institution	Science Interactive University
Session	SI Physics - Full Discipline Demo
Course	SI Physics - Full Discipline Demo
Instructor	Sales SI Demo

Test Your Knowledge

Order the materials from smallest refractive index to largest refractive index.

≡ Air	1 Correct answer: Air
≡ Diamond	2 Correct answer: Water
≡ Glass	3 Correct answer: Quartz
≡ Quartz	4 Correct answer: Glass
≡ Water	5 Correct answer: Diamond

Match each term with the best description.

⚡ Dispersion	Ratio of the speed of light in a vacuum to the speed of light in a medium	1
⚡ Ray	Rule for how light is refracted at the boundary between two materials	2
⚡ Refractive index	Process that occurs when the angle of incidence is greater than the critical angle	3
⚡ Snell's law	Path of a particle of light	4
⚡ Total internal reflection	The separation of light into different frequencies to produce a rainbow	5

Correct answers:

- 1 Refractive index 2 Snell's law 3 Total internal reflection 4 Ray
5 Dispersion

Categorize each statement as true or false.

⚡ At the critical angle, no light is reflected and all light is transmitted.	
⚡ During refraction, the ray that travels through the second medium is called the incident ray.	
⚡ The angle of refraction is measured from the perpendicular to the boundary between two materials.	
⚡ The speed of light in a medium is always less than the speed of light in a vacuum.	
⚡ The virtual image of a pencil in a glass of water is closer to the viewer than the actual pencil.	
True	False
1	2

Correct answers:

1

The angle of refraction is measured from the perpendicular to the boundary between two materials.

The speed of light in a medium is always less than the speed of light in a vacuum.

The virtual image of a pencil in a glass of water is closer to the viewer than the actual pencil.

2 At the critical angle, no light is reflected and all light is transmitted.

During refraction, the ray that travels through the second medium is called the incident ray.

Exploration

Light is an electromagnetic wave and also a discrete particle.

- ☒ True ✓
- ☐ False

The index of refraction depends on the ____.

- ☐ speed of light in the medium
- ☐ frequency of light
- ☐ density of the medium
- ☒ All of the above ✓

Light bends when it enters a new medium because of its change in ____ as it crosses the boundary.

- ☒ speed ✓
- ☐ frequency
- ☐ color
- ☐ All of the above

The bending of light as it passes from one medium to another is called ____.

- ☐ reflection
- ☐ transmission
- ☒ refraction ✓
- ☐ All of the above

The angles of incidence and refraction are measured from the ____ of the boundary between two materials.

- ☐ parallel
- ☒ normal ✓
- ☐ 45 degree
- ☐ All of the above

Snell's law depends on the refractive indexes of the materials as well as on the ____ of the angles of the light rays.

- ☐ square roots
- ☒ sines ✓
- ☐ cosines
- ☐ None of the above

Total internal reflection occurs only when n_2 is ____ n_1 .

- ☒ less than ✓
- ☐ equal to
- ☐ greater than
- ☐ All of the above

The cladding of a fiber optic cable has a refractive index ____ the refractive index of the central glass cable.

- ☒ less than ✓
- ☐ equal to
- ☐ greater than
- ☐ None of the above

The angle of refraction for light passing from water into air is ____ the angle of incidence, causing the broken appearance of a pencil in a glass of water.

- ☐ less than
- ☐ equal to
- ☒ greater than
- ☐ None of the above

✓

A virtual image ____ appears on a screen placed at the location of the image.

- ☐ always
- ☒ never
- ☐ sometimes
- ☐ None of the above

✓

Exercise 1

What is the relationship between the incident angle at the top of the block and the refracted angle at the bottom of the block? Explain using Snell's law and Data Table 1.

The incident angle at the top of the block and the refracted angle at the bottom of the block are very similar for all trials, all within 1.5° . So, the ray that enters the block and the ray that leaves the block are parallel. This is reflected by Snell's law and simple geometry. Since the block's sides are parallel, the angles measured from each normal (θ_{iT} and θ_{iB}), if done correctly, should be identical. Thus, Snell's law, which states $n_{air}\sin(\theta_{iT})=n_{block}\sin(\theta_{rT})$ and $n_{block}\sin(\theta_{iB})=n_{air}\sin(\theta_{rB})$. Since θ_{rT} and θ_{iB} are identical, this can be simplified as $n_{air}\sin(\theta_{iT})=n_{air}\sin(\theta_{rB})$. Since the index of refraction is the same, this equation implies $\theta_{iT} = \theta_{rB}$. Thus the ray entering the block and the ray leaving the block are parallel.

Why must the slope of your graph in Graph 1 be greater than 1? What would a slope of less than 1 indicate? Consider the definition of index of refraction.

The slope must be greater than 1 because the index of refraction must always be greater than one. The index of refraction is defined as the ratio of the speed of light in vacuum to the speed of light in a material. The speed of light in a material can never exceed the speed in vacuum, meaning the index of refraction can never be greater than 1.

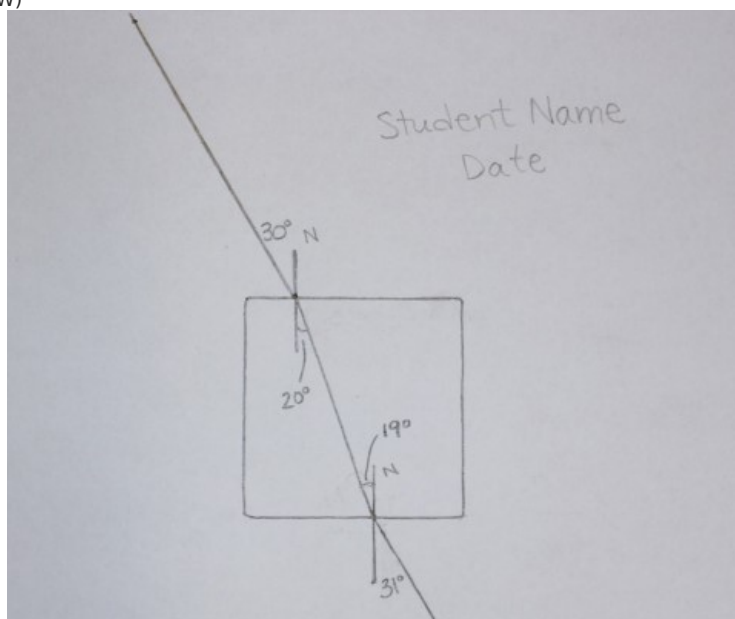
What is the index of refraction of an unknown material if a light ray travels from water ($n=1.33$) at an incident angle of 30° from the normal and bends in the material at an angle 20° from the normal? Show all calculations in your answer.

Snell's law states: $n_1 \sin \theta_1 = n_2 \sin \theta_2$. This can be rearranged to be: $n_2 = n_1 \sin \theta_1 / \sin \theta_2$. So: $n_2 = 1.33 \sin(30) / \sin(20) = 1.33 * 0.5 / 0.34 = 1.94$.

Data Table 1: Index of Refraction from Individual Incident Angles
(SAMPLE ANSWER BELOW)

Incident Angle θ_{iT} ($^\circ$)	Refracted Angle θ_{rT} ($^\circ$)	Incident Angle θ_{iB} ($^\circ$)	Refracted Angle θ_{rB} ($^\circ$)	Index of Refraction (from top)	Percent Error (from top) (%)	Index of Refraction (from bottom)	Percent Error (from bottom) (%)
30	20.0	19.0	31.0	1.46	1.89	1.58	6.17
45	29.0	28.0	45.5	1.46	2.11	1.52	1.96
60	37.0	36.0	61.5	1.44	3.42	1.50	0.34

Photo 1: Incident Angle of 30°
(SAMPLE ANSWER BELOW)



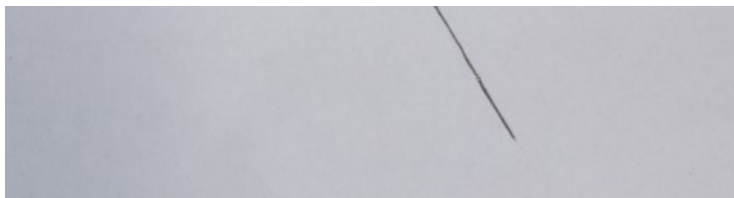


Photo 2: Incident Angle of 45°
(SAMPLE ANSWER BELOW)

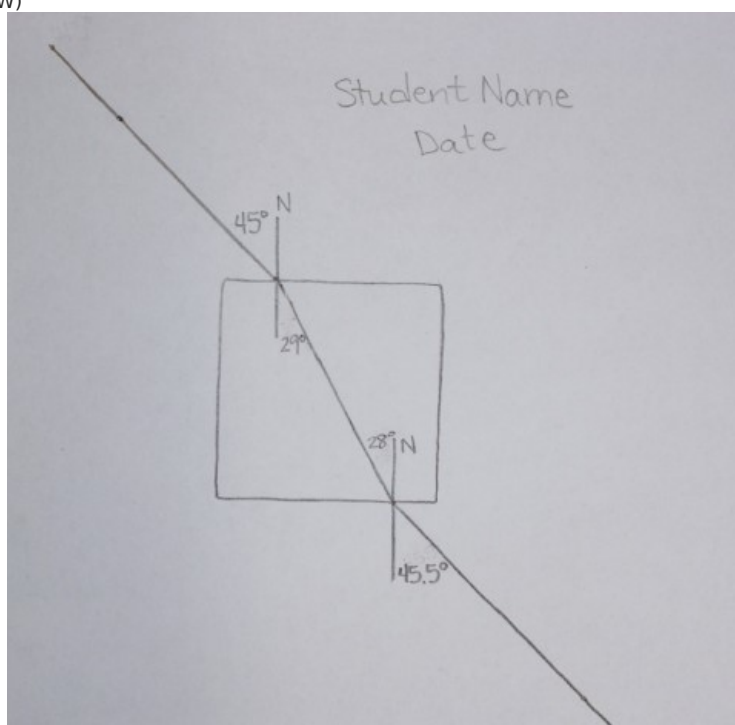
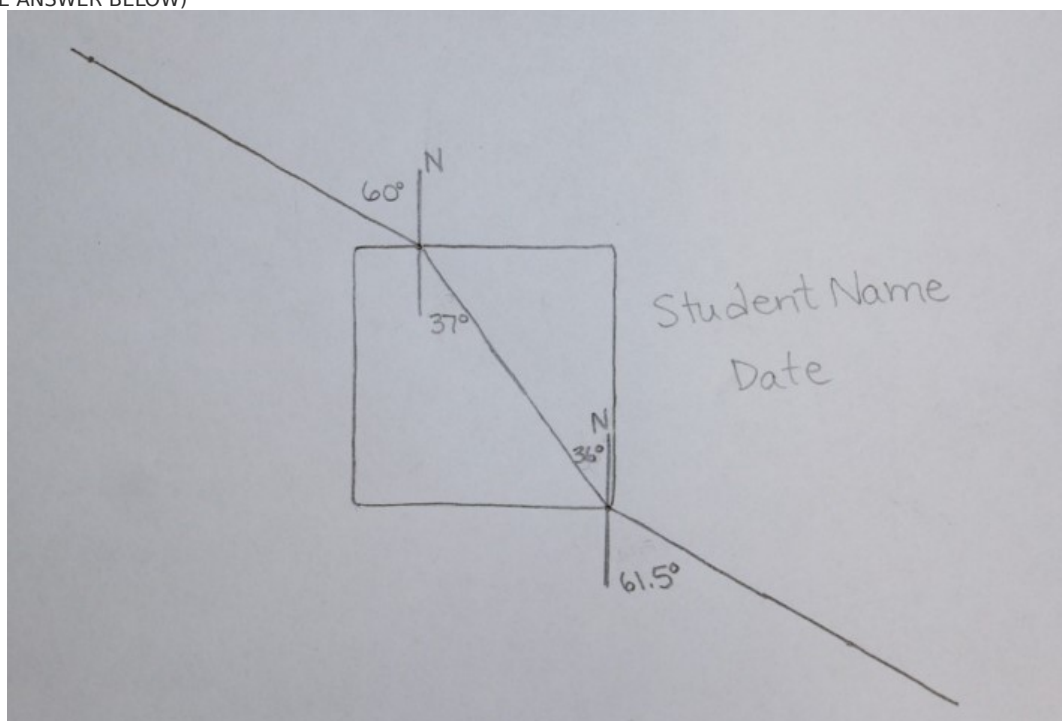




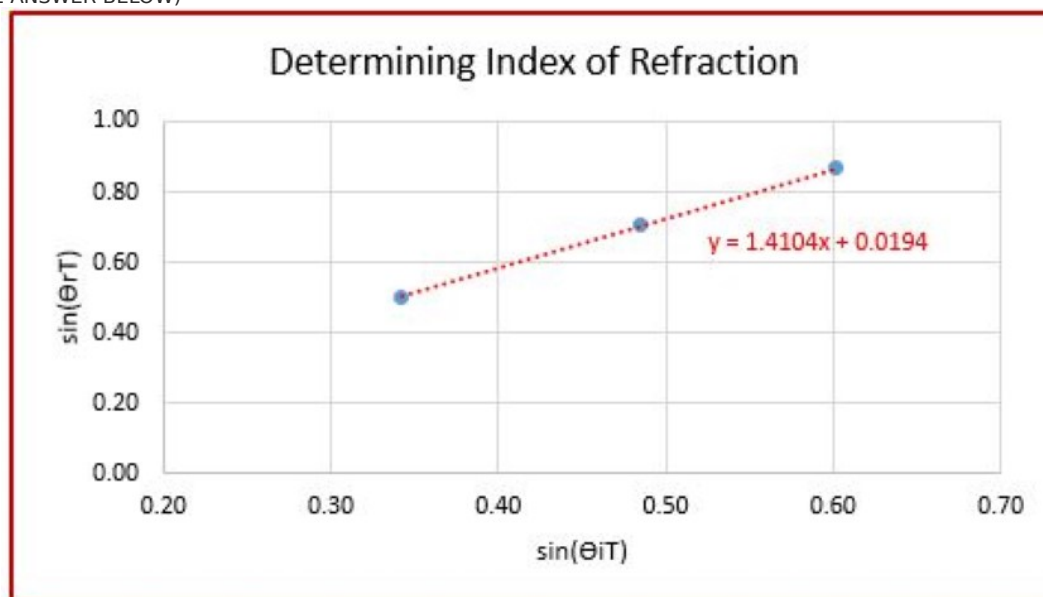
Photo 3: Incident Angle of 60°
(SAMPLE ANSWER BELOW)



Data Table 2: Index of Refraction with the slope of a Graph
(SAMPLE ANSWER BELOW)

Incident Angle θ_{iT} (°)	Refracted Angle θ_{rT} (°)	$\sin(\theta_{iT})$	$\sin(\theta_{rT})$	Index of Refraction	Percent Error (%)
30	20.0	0.50	0.34	1.41	5.37
45	29.0	0.71	0.48		
60	37.0	0.87	0.60		

Graph 1: Index of Refraction
(SAMPLE ANSWER BELOW)



Exercise 2

Would total internal reflection occur if the top material was air and the bottom material was water? Explain your answer using the equation for critical angle.

No. Total internal reflection (TIR) cannot occur when light travels from a material of lower index of refraction to higher index of refraction. This is a direct result of the equation used to find the critical angle: $\theta_c = \arcsin(n_{\text{bottom}}/n_{\text{top}})$, when entering from the top material to the bottom material. If the index of refraction of the bottom of the material is larger than that of the top material, the ratio of refractive indices inside the arcsine is greater than 1. However, the value of sine can never exceed 1. So, the bottom material's index of refraction must be larger for TIR to occur. Since air has a lower index of refraction than water, TIR can never occur when light travels from air to water (but does from water to air).

What is the critical angle for a ray of light traveling from glass (n=1.5) to water (n=1.33)? Show all calculations in your answer.

$$\theta_c = \arcsin(n_2/n_1) = \arcsin(1.33/1.5) = \arcsin(0.887) = 62.5^\circ.$$

Data Table 3: Determining Critical Angle
(SAMPLE ANSWER BELOW)

Material	Index of Refraction	Measured Critical Angle (°)	Calculated Critical Angle (°)
Water	1.33	49	48.8
Glass	1.50	42	41.8

Data Table 4: Determining Index of Refraction from Critical Angle
(SAMPLE ANSWER BELOW)

Material	Measured Critical Angle (°)	Index of Refraction	Predicted Material
Mystery A	25	2.37	Diamond
Mystery B	46	1.39	Sellaite

Competency Review

The index of refraction is always less than or equal to one.

- ☐ True
- ☒ False ✓

The ray that passes from one medium to another during refraction is called the ____ ray.

- ☐ transmitted
- ☐ reflected
- ☒ refracted ✓
- ☐ None of the above

According to Snell's law, the medium with the larger index of refraction will have the larger angle.

- ☐ True
 - ☒ False
- ✓

Snell's law can be used to solve for the index of refraction of a medium if the ____ is known.

- ☐ angle of incidence
 - ☐ angle of refraction
 - ☐ index of refraction of the other medium
 - ☒ All of the above
- ✓

Total internal reflection occurs when the angle of incidence is ____ the critical angle.

- ☐ greater than
 - ☐ equal to
 - ☒ greater than or equal to
 - ☐ None of the above
- ✓

Total internal reflection is possible when light travels from air into water.

- ☐ True
 - ☒ False
- ✓

The critical angle for total internal reflection is the angle of incidence that causes an angle of refraction of exactly ____ degrees.

- ☒ 90
 - ☐ 45
 - ☐ 0
 - ☐ None of the above
- ✓

The virtual image of a fish in a pond as viewed from above the pond is ____ the surface than the actual location of the fish in the pond.

- ☒ closer to ✓
- ☐ farther from
- ☐ perpendicular to
- ☐ None of the above

When n_2 is greater than n_1 , the image distance will be ____ the object distance.

- ☐ less than
- ☒ greater than ✓
- ☐ equal to
- ☐ None of the above

For an object in water with a refractive index of 1.33 located 1.0 meters from an observer in air with a refractive index of 1.0, the image distance is ____ meters.

- ☐ 0.67
- ☐ 1.33
- ☒ 0.75 ✓
- ☐ None of the above

When light passes through a rectangular block the emergent ray is parallel to the ____ ray.

- ☐ refracted
- ☒ incident ✓
- ☐ reflected
- ☐ None of the above

The refracted angle at the top of a refraction block is ____ the incident angle at the bottom of the block.

- ☐ greater than
- ☐ less than
- ☒ equal to ✓
- ☐ None of the above

The incident angle for a light ray traveling from water ($n=1.33$) into an unknown substance is 30 degrees. The refraction angle is 21 degrees so the index of refraction for the unknown substance is ____.

- ☐ 1
- ☒ 1.9 ✓
- ☐ 1.4
- ☐ None of the above

When the slope of a graph is the index of refraction for a material and light is refracted from air into that material, the vertical axis of the graph is ____.

- ☒ the sine of the angle of incidence ✓
- ☐ the angle of incidence
- ☐ the sine of the angle of refraction
- ☐ None of the above

Sapphire has an index of refraction of 1.77. The critical angle for sapphire in air with an index of refraction of 1.0 is ____ degrees.

- ☐ 3
- ☐ 90
- ☒ 34 ✓
- ☐ None of the above

Total internal reflection will not occur for any angle when light shines from air ($n=1.0$) into a sapphire ($n = 1.77$).

- ☒ True ✓
- ☐ False

An unknown substance has a critical angle of 43 degrees, so its index of refraction is ____.

- ☒ 1.47 ✓
- ☐ 1.33
- ☐ 1
- ☐ None of the above

Total internal reflection only occurs when the second medium ____.

- ☐ is air
- ☒ has an index of refraction less than the first medium ✓
- ☐ has an index of refraction greater than the first medium
- ☐ None of the above

Extension Questions

Does a fish appear closer or farther from a person wearing swim goggles with an air pocket in front of their eyes than the fish really is? Does the fish see the person's face closer or farther than it really is? Explain your answer. (SAMPLE ANSWER BELOW)

The fish appears closer than it really is because light from the fish is refracted away from the normal as it enters the air pocket in the goggles. This is because air has a smaller index of refraction than water. The person will trace rays back to an image point in front of the actual fish. The fish will see the person's face exactly where it actually is because the light from the face is not refracted as it travels through water only, and does not change from one medium to another.

Light rays from stars bend toward smaller angles as they enter Earth's atmosphere. a. Explain why this happens using Snell's law and the speed of light. b. Where are the actual stars in relation to their apparent position as viewed from the Earth's surface? (SAMPLE ANSWER BELOW)

a. Snell's law says that the angle of refraction will be smaller than the angle of incidence when the index of refraction of the second medium is greater than that of the first. Light from stars enters the atmosphere from the vacuum of space, so the index of refraction of the atmosphere is greater than that of a vacuum. The index of refraction of a vacuum is one exactly, while it is slightly

greater than 1 for the atmosphere. This is because the speed of light in a vacuum is c , and the speed of light in the atmosphere is a little bit lower than c . b. The actual stars are slightly closer than they appear as viewed through the atmosphere because the image distance is larger than the object distance when the index of refraction of the second medium is larger than that of the first medium.
